Design & Simulation of Fuzzy Logic Based Speed Control of SPWM Inverter-fed Electrical Vehicle with Induction Motor taking Core loss and Stray Load Losses into Account

Sadia Nahar, Md. Kamrul Hassan, Mohammad Abdul Mannan

Abstract — In modern technology electrical differentials to design Electrical Vehicle (EV) are getting popular for its simplicity, faster response, accurate control capability and other facility. The controller design for the distinctive motors is a captivating and challenging work to acquire sought execution appropriately. For this different kind of controller is used to get accurate results. For Induction Motor (IM) it is very important to control the speed and torque to get smooth control application. Field Oriented Control (FOC) aids the factor and empowers independent control of speed and torque by building up an autonomous relationship is created due to consideration of core loss and stray load losses while modeling Induction Motor which is neglected at most of the works. Here, Induction Motor is modeled with the Fuzzy Logic Controller for more accuracy and simplicity and the Sinusoidal Pulse Width Modulation (SPWM) is utilized as a part of the structure to investigate the performance of IM under various source parameters such as diversity of voltage, frequency and so forth. MATLAB/Simulink is used to execute the simulation results.

Keywords— Electrical Vehicle; Induction Motor; Fuzzy Logic Controller; Sinusoidal Pulse Width Modulation; Field Oriented Control;

I. INTRODUCTION

With the height of technological headway in current time, the automotive engineering faced a lot progressive dealing of side by side innovations. The developing concern with the unfriendly impacts of hydrocarbon-related vehicle, electronic vehicles have benefitted prominent position in cutting edge time. Over the time progression in innovation has occurred; manufacturers incorporate more and more attractive than before [1]. So the attention concentrated on autonomous driving wheel engine on the back wheel to supplanted Mechanical Differential (MD) into Electrical Differential (ED) in EV [1, 2]. ED constitutes an innovative advancement in vehicle design decreasing the vehicle mass and improving the overall system reliability and efficiency [2, 3]. ED's principle feature is the robust improvement against system uncertainties and street conditions. ED can control both the driving wheel independently to turn at different speed in any curve and distribute the power to each motor according to the steering angle [3].

Induction Motor is very popular in the industrial applications because of its low maintenance and cost, simplicity of design, robustness, good self starting, high efficiency, small inertia and absence of the controller brooms system [4-6]. Field Oriented Control (FOC) accompanies the state of legitimate modeling of IM. Induction motors are modeled from various perspectives. Each of it has claim favorable position and burden. In any case, to acquire a consummately working control scheme, it is vital that the system under supervision is modeled appropriately so that maximum of its behavior can be anticipated.

Induction motor models are considered without taking the core loss and stray load losses into account in most of works [6-9]. Therefore, greater portion of the speed controllers designed so far could not achieve expected performance and hence failed to produce satisfactory output. However, some recent work takes core loss and stray load loss into account [10-13]. These are so far the most effective models of induction motor which can be expected to work with accuracy.

In order to achieve the same performance of DC machine from IM, the rotor flux and torque are decoupled in terms of stator current components neglecting the core loss and stray load losses. These losses of induction motor are very common and may not be negligible to achieve precise industrial application. To design the precise control strategies of an IM considering core loss and stray load losses different mathematical model based on the equivalent circuit has been reported in literatures. Core loss was represented by an equivalent resistance in parallel with the magnetizing branch [10-13] and stray load loss was represented by a resistance in parallel with the secondary leakage inductance [10-13]. The

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Fuzzy-Logic Control (FLC) is seemed to be a suitable controller in terms of high dynamic response under the variation of load torque and parameters [12, 13]. The FLC get its popularity due to its simple linguistic rules like human thinking. It does not need any precise mathematical explanations to obtain a decision inference. The FLC requires only a qualitative knowledge which not only makes to controller easy to use but also easy to design. So it eases obtaining speed controller for an IM.

This paper proposes a fuzzy logic control application of an electrical differential system for an EV propelled by two IM (One for each rear wheel). Overall system including FLC with IM taking core loss and stray load losses into account is implemented in MATLAB Simulink.

II. DYNAMIC & STATE SPACE MODEL OF INDUCTION MOTOR

The dynamic modeling of an IM taking core loss and stray load losses into account in synchronously rotating d-q axis reference frame is shown in Fig. 1. The reference frame is rotating of an electrical angular velocity \( \omega_e \). Hysteresis loss and eddy current loss are the two components of core loss but for simplicity, the components of core loss are represented by a single quantity with a constant value of \( R_e \) and stray load losses are shown with constant value \( R_st \) as shown in Fig. 1.

\[
\begin{align*}
\frac{dS}{dt} &= -K_{20}i_s - K_{21}i_m - K_{22}\Phi_r - j\omega_{se}i_s - jK_{23}\omega_rei_m + K_{19}v_s - K_{24}v_r \\
\frac{di_m}{dt} &= K_{14}i_s + K_{15}i_m + K_{16}\Phi_r + jK_{17}\omega_rei_m - j\omega_{se}i_m + K_{18}v_r \\
\frac{d\Phi_r}{dt} &= K_{25}i_s - K_{26}i_m - K_{27}\Phi_r - jK_{28}\omega_rei_m - j\omega_{se}i_m + K_{19}v_r \\
\frac{d\omega_{re}}{dt} &= -K_{30}\omega_{re} + K_{31}(T_e - T_L) \\
T_e &= \left(\frac{3}{2}\right)P_n[i_{rd}\Phi_{rq} - i_{rq}\Phi_{rd}] 
\end{align*}
\]

Here,
\[
\begin{align*}
K_8 &= \frac{R_c}{R_{rsc}}; \\
K_9 &= \frac{R_c}{R_{rsc}L_m}; \\
K_{10} &= \frac{R_{st}}{R_{rsc}L_{rt}}; \\
K_{11} &= \frac{L_m}{R_{rsc}}; \\
K_{12} &= \frac{(R_{rsc} - R_c)R_c}{R_{rsc}L_m}; \\
K_{15} &= \frac{R_c}{R_{rsc}L_{rt}}; \\
K_{16} &= \frac{R_c}{R_{rsc}L_{rt}}; \\
K_{17} &= \frac{R_c}{R_{rsc}}; \\
K_{18} &= \frac{R_c}{R_{rsc}L_m}; \\
K_{19} &= \frac{1}{L_{st}}; \\
K_{20} &= \frac{R_{rsc} + R_{rsc}R_c}{R_{rsc}L_{st}}; \\
K_{21} &= \frac{R_cR_{st}}{L_{sl}} \left(\frac{R_cL_{rt} - R_{rt}L_m}{R_{rsc}L_{rt}} - 1\right);
\end{align*}
\]

According to Fig. 1 the d-q axis stator voltage of an IM as follows:
\[
\begin{align*}
v_s &= R_si_s + (L_{st}\omega seL_{st}i_s) + (L_m\omega seL_{ml}i_m) \\
v_r &= R ri_r + (L_{rt}\omega seL_{rt}i_r) + (j(\omega se - \omega re)L_rLi_r) + (jL_m\omega seL_{ml}i_mL_{st}) - j\omega reL_{ml}i_ml \\
\Phi_s &= L_{st}i_s + L_mi_m \\
\Phi_r &= L_{rt}i_r + L_mi_m
\end{align*}
\]

For squirrel cage motor,
\[
\begin{align*}
R_c i_c &= L_m\frac{di_m}{dt} + j\omega seL_m i_m \\
R_{st}i_{st} &= L_{rt}\frac{di_r}{dt} + j\omega seL_{rt}i_r \\
i_s + i_r &= i_c + i_m \\
T_e &= \left(\frac{3}{2}\right)P_n(\Phi_{qr}i_{dr} - \Phi_{dr}i_{qr}) \\
i_{st} &= i_r - i_l \\
\end{align*}
\]
\[ K_{22} = \frac{R_c R_{st}}{R_{rsc} L_{rl} L_{sl}} \; ; \; K_{23} = \frac{R_c L_m}{R_{rsc} L_{rl}} \; ; \]
\[ K_{24} = \frac{R_c}{R_{rsc} L_{sl}} \; ; \; K_{25} = \frac{R_c R_{r}}{R_{rsc}} \; ; \]
\[ K_{26} = \frac{R_c (R_{r} L_{rt} - R_{st} L_{rl})}{R_{rsc} L_{rl}} \; ; \; K_{27} = \frac{R_c R_{st}}{R_{rsc} L_{rl}} \; ; \]
\[ K_{28} = \frac{R_c L_{m}}{R_{rsc}} \; ; \; K_{29} = 1 - \frac{R_c}{R_{rsc}} \; ; \; K_{30} = \frac{B_m}{J_m} \; ; \; K_{31} = \frac{P_n}{J_m} \; ; \; K_{32} = \frac{3}{2} P_n K_{31} \]

### III. ELECTRICAL VEHICLMECHANICAL LOAD

Here, the load is the vehicle and it is characterized by different resistive torques. The vehicle torques are given below [14, 15]:

- The rolling force and torque can be given as:
  \[
  \begin{align*}
  F_{roll} &= M g f_r \\
  T_{roll} &= M g f_r R \omega 
  \end{align*}
  \]

- The aerodynamic force and torque is:
  \[
  \begin{align*}
  F_{aero} &= \frac{1}{2} \rho A_f C_d v_h^2 \\
  T_{aero} &= \frac{1}{2} \rho A_f C_d v_h^2 R \omega
  \end{align*}
  \]

- The slope force and torque can be given as:
  \[
  \begin{align*}
  F_{slope} &= M g \sin \beta \\
  T_{slope} &= M g \sin \beta R \omega
  \end{align*}
  \]

- The total resistive torque can be defined as:
  \[
  T_{res} = T_{roll} + T_{aero} + T_{slope}
  \]

### IV. ELECTRONIC DIFFERENTIAL MODELING

The proposed control system principle could be summarized as follows: 1) Speed control is used to control each motor torque; 2) The speed of each rear wheel is controlled using speed difference feedback. Here, the two rear wheels are driven by two separate motors.

For steering condition, when the vehicle need to turn right then the left wheels speed will be higher than the right wheel and vice versa.

Here, the Ackermann-Jeanutaud steering model driving trajectory is used for the vehicle systems model analysis [15].

\[ v_L \] is the linear speed of the left wheel drive; \( v_R \) is the right wheel drive. The linear speed of each wheel drive is expressed as a function of the vehicle angular speed and the radius of the curve, according to Fig. 3.
When the steering angle is applied the speed of inner wheel is reduced and the speed is increased of outer wheel. The driving wheel reference angular speeds are calculated by:

\[
\omega_{1R} = \omega_p + \frac{\Delta \omega}{2} \quad \text{and} \quad \omega_{2R} = \omega_p - \frac{\Delta \omega}{2}
\]  

The speed references of the two motors are:

\[
\omega_{1m} = k_{gear}\omega_{1R} \quad \text{and} \quad \omega_{2m} = k_{gear}\omega_{2R}
\]

Where, \( k_{gear} \) is the gearbox ratio.

\[\text{Fig. 4: Block Diagram to Show the Use of the Electronic Differentiator.}\]

V. FUZZY LOGIC CONTROLLER

One reason for the ubiquity of Fuzzy Logic Controllers (FLC) is its logical similarity to a human operator. Not like other control systems, this is less difficult as there is no complex mathematical learning required. The FLC requires only qualitative information of the framework subsequently making the controller simple to use, as well as to design. Fig. 5 shows the simplified block diagram of FLC. Three essential parts of FLC are:

A. Fuzzification:

The fuzzification step converts the numerical input variables into linguistic variables by the fuzzifier. The controllers input linguistic variables available are the difference of the actual speed from the desired or reference speed, \( e\omega(k) \) and the difference of speed error, \( \Delta e\omega(k) \) and the first difference of magnetizing q-axis current \( \Delta i_{mq}^* \), is considered as the output linguistic variable. To ease the equations, the input and output are scaled with different coefficients these are: \( K_{e\omega} \) error of speed; \( K_e \) change of error of speed and \( K_i \) first difference of magnetizing q-axis current. Here the scaling factors are considered as constant and are selected by trial and error.

\[\text{Fig. 5: Simplified Block Diagram of Fuzzy logic Controller.}\]

B. Rule Base:

The fuzzy mapping of the input variables to the output is represented to fuzzy IF-THEN rules of the following form:

If \( (e_{\omega}^n \text{ is } N) \) and \( (\Delta e_{\omega}^n \text{ is } N) \) Then \( (\Delta i_{mq}^n \text{ is } S) \)

If \( (e_{\omega}^n \text{ is } P) \) and \( (\Delta e_{\omega}^n \text{ is } Z) \) Then \( (\Delta i_{mq}^n \text{ is } B) \)

The entire rule base is given in Table I. There are total 49 rules to acheive desired speed trajectory.

C. Interface and Defuzzification:

The Inference system provides fuzzy values of \( \Delta i_{mq}^n \) from the rule base in Table I and then crisp numerical value of \( \Delta i_{mq}^n \) is obtained by using defuzzification procedure. Here it is done with the most popular method of inference and difuzzification Mamdani’s max-min (or sum-product) composition with center of gravity method.

\[\text{Fig. 6: Scheme structure of the proposed FLC.}\]

\[\text{Fig. 7: Fuzzy sets and their corresponding membership function.}\]

{| Table I. Fuzzy Rules | $\Delta e_{\omega}^n$ | $\Delta i_{mq}^n$ |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Delta i_{mq}^n$</td>
<td>NB</td>
<td>NM</td>
</tr>
<tr>
<td>$e_{\omega}^n$</td>
<td>NB</td>
<td>NB</td>
</tr>
<tr>
<td>NM</td>
<td>NB</td>
<td>NB</td>
</tr>
<tr>
<td>NS</td>
<td>NM</td>
<td>NM</td>
</tr>
<tr>
<td>GS</td>
<td>GS</td>
<td>GS</td>
</tr>
<tr>
<td>GS</td>
<td>GS</td>
<td>GS</td>
</tr>
</tbody>
</table>

The 49 rules shown in tabular form are written in the program according to the syntax provided by MATLAB. The document is saved with the extension ‘.fis’

VI. SPWM INVERTER DESIGN

In the Sinusoidal Pulse-Width-Modulation (SPWM) modulation technique, the width of pulse is varied in proportion to the amplitude of a sine-wave evaluated at the center of the same pulse [16]. The gating signals are generated by comparing
a sinusoidal reference signal of frequency, with a triangular carrier wave of frequency. Here, the reference voltages $U_a$, $U_b$, $U_c$ were taken from the controller to compare with triangular signal according to the Sinusoidal Pulse Width Modulation (SPWM) Techniques. Fig. 8 shows the pulses $S_a$, $S_b$ and $S_c$, which generated by comparing the voltages $U_a$, $U_b$, $U_c$ with triangular wave.

The desired Voltages $V_a$, $V_b$, $V_c$ can calculated based on the generated gate pulses using following equations:

$$
\begin{bmatrix}
V_a \\
V_b \\
V_c
\end{bmatrix} = \frac{U_{dc}}{2} \begin{bmatrix}
2 & -1 & -1 \\
-1 & 2 & -1 \\
-1 & -1 & 2
\end{bmatrix} \begin{bmatrix}
S_a \\
S_b \\
S_c
\end{bmatrix} \quad \cdots (29)
$$

In this paper Matlab/Simulink in used to solve those equations to get desired voltages.

VII. SIMULATION & RESULTS

The performance of the proposed control system is simulated using Matlab/Simulink software. The used parameters for simulation are shown in Appendix 1 and Appendix 2. For this simulation the sampling time is chosen to be 100µs. The desired goal of this proposed scheme is to see the performance for slope road condition.

A. Slope (up-hill and down-hill) Road Condition

Fig. 9 and Fig. 10 show the transient simulation results of speed (Load) and torque (Electromagnetic Torque) for the slope condition. Here, the vehicle is considered to be running on up-hill and down-hill condition. When the vehicle runs in up-hill condition then the slope torque is positive and overall torque is increased. In the Fig. 10 (a) and (b) at $t = 2.5s$, the vehicle is running uphill so the both motors torque increases. Again when the vehicle runs in down-hill condition then the slope torque is negative and overall torque is decreased. Like the Fig. 10 (a) and (b) shows at $t = 6s$, the vehicle goes down-hill so the torque of the both motor decreases. When the vehicle goes to up-hill direction, the load torque increased as shown in Fig. 10 (a) and (b), and due to the increase of load torque the speed is fall down as shown in Fig. 9 (a) and (b) at $t = 2.5s$. Similar to that when the torque is decreased means the vehicle is going down-hill the speed of the both vehicle increased at $t = 6s$. 
VIII. Conclusion

This paper has discussed about the model of an Electrical Vehicle, including model of IM taking core loss and stray load losses with a Fuzzy Logic Controller. The whole simulation is done incorporate with SPWM in Matlab environment. The proposed method shows the results for slope road condition only. The proposed controller is skilled to give a superior performance both at transient and steady state condition. It overcomes the problem of overshoot and load torque change that was present in case of PI controller. Also it comforts the designer since it is free from tiring mathematical expressions. More works should be done to simulate the other road conditions on this proposed method.

APPENDIX 1. RATINGS AND PARAMETERS OF INDUCTION MOTOR

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_s$</td>
<td>85.1 m$\Omega$</td>
</tr>
<tr>
<td>$R_r$</td>
<td>65.8 m$\Omega$</td>
</tr>
<tr>
<td>$R_c$</td>
<td>812 $\Omega$, $R_{m}$= 5.2 $\Omega$</td>
</tr>
</tbody>
</table>

$L_{sl} = 2.3$ mH, $L_{lr} = 1.5$ mH, $L_m = 29.1$ mH,
$J = 0.23$ Kg·m$^2$

APPENDIX 2. EV MECHANICAL AND AERODYNAMIC PARAMETERS

$M = 1300$ kg; $A = 2.6$ m$^2$; $R_w = 0.32$ m;
$C_d = 0.32; \eta = 0.98; v = 22.2$ m/s;
$g = 9.81$ m/s$^2$; $\rho = 1.2$ kg/m$^2$.

REFERENCES


Sadia Nahar was born in Dhaka, Bangladesh on July 16, 1992. She received her B.Sc. Eng. Degree in EEE from American International University-Bangladesh (AIUB), Bangladesh in 2014. At present, she is doing her Masters in Electrical & Electronic Engineering in EEE Department of American International University-Bangladesh (AIUB), Bangladesh.

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